

The Pion Form Factor

Present status and future outlook

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European Research Conference

on

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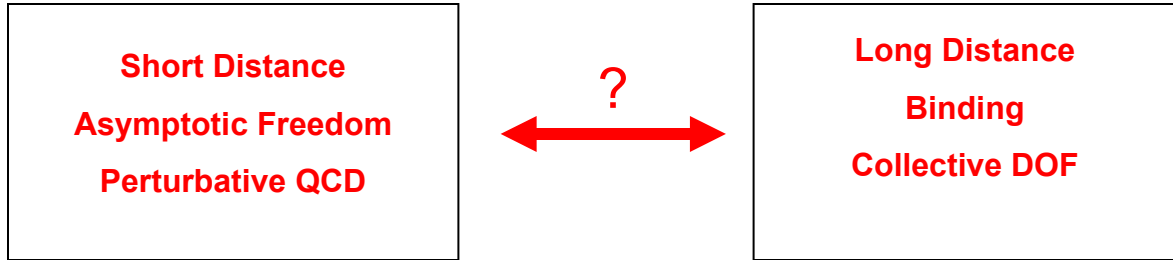
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BUT, we are unable to construct a quantitative description of hadrons in terms of the underlying constituents, quarks and gluons.

- We know that there is an asymptotic limit, but how do we get there and what governs the transition?



ables for understanding hadronic structure

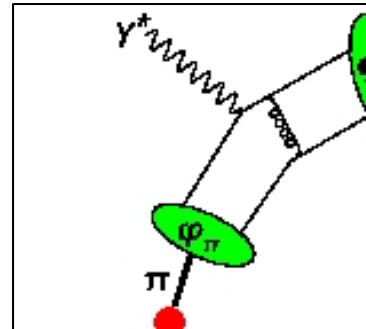
Simple qq valence structure of π^+

The pQCD description is expected to be valid at much lower values Q^2 compared to the nucleon

very large Q^2 one can calculate F_π in pQCD, which reduces to normalized form as $Q^2 \rightarrow \infty$

$$F_\pi(Q^2) \rightarrow 16\pi \frac{\alpha_s f_\pi^2}{Q^2}$$

where $f_\pi=93 \text{ MeV}$ is the $\pi^+ \rightarrow \mu^+ \nu$ decay constant



This asymptotic normalization does

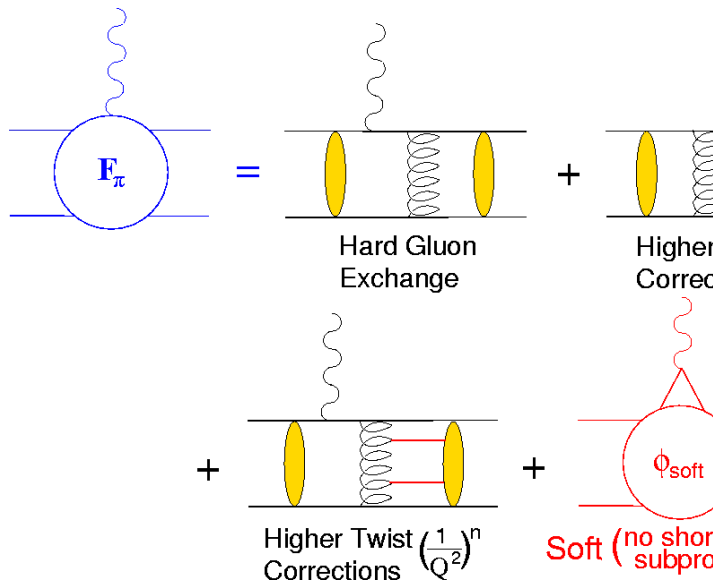
phenomenally accessible Q^2
hard and soft components
contribute

transverse momentum effects

interplay of hard and soft
components is not well
understood

non-perturbative hard
components of higher twist cancel
soft components [V. Braun et al.,
PRD **61** (2000) 07300]

different theoretical perspectives
on dominance of higher twist



the charged pion presents a clean test case for our understanding of bound quark systems

Structure of pion at all Q^2 values

what value of Q^2 will hard pQCD contributions dominate?

Perturbative QCD(LO) hard calculations under-predict experimental data by a factor of 2-3

many studies of F_π , but the interplay of hard and soft contributions is not well understood

Constraints on theoretical models require high precision data

JLab is the only experimental facility capable of the necessary measurements

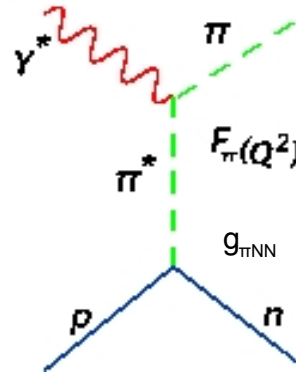
- Accurate measure of the π^+ charge radius, $r_\pi = 0.657 \pm 0.012$ fm

At larger Q^2 values, one must use the “virtual pion cloud” of the proton to extend the F_π measurement

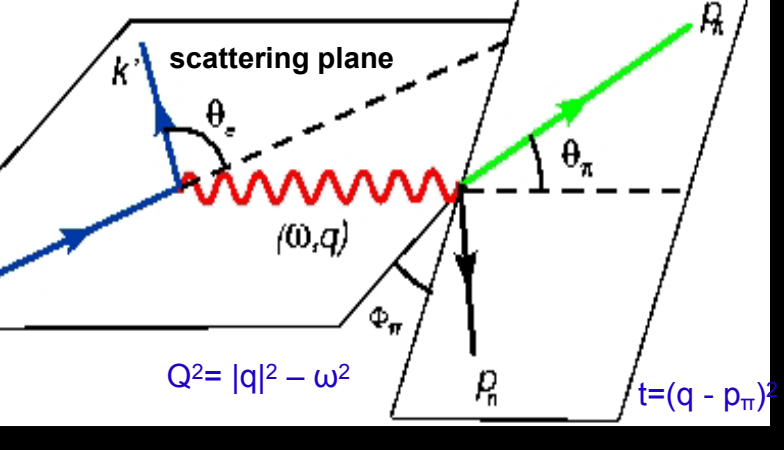
- t-channel diagram dominates σ_L at small $-t$

In the Born term model:

$$\frac{d\sigma_L}{dt} \propto \frac{-tQ^2}{(t - m_\pi^2)} g_{\pi NN}^2(t) F_\pi^2(Q^2, t)$$



Pion electroproduction



dominance of σ_L

- For maximum contribution to σ_L , need dominance of the π^+ pole to σ_L , need dominance of the smallest possible $-t$
- At fixed Q^2 , a higher value of ω allows for smaller $-t_{\min}$

Extraction of F_π requires knowledge of the $-t$ dependence of σ_L

Only three of Q^2 , W , t , and θ_π are independent

Must vary θ_π to measure the $-t$ dependence (off-parallel)

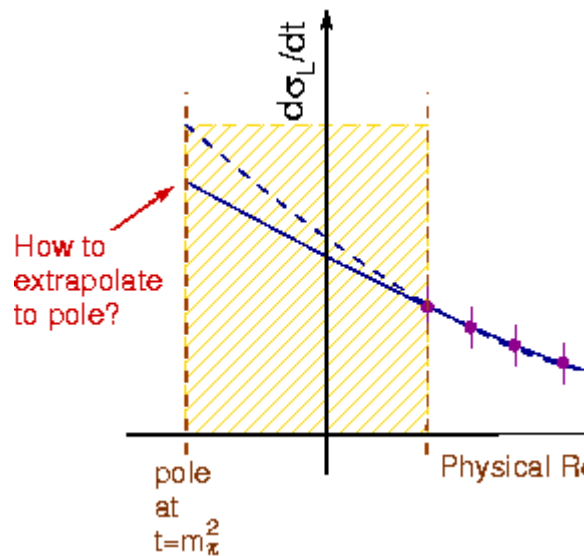
In off-parallel kinematics LT and TT must also be determined

$-t > 0$ (away from the $-t = m_\pi^2$
e)

Early experiments used “Chew-
Low” extrapolation technique

Need to know the $-t$
dependence through the
unphysical region

A reliable extrapolation is not
possible

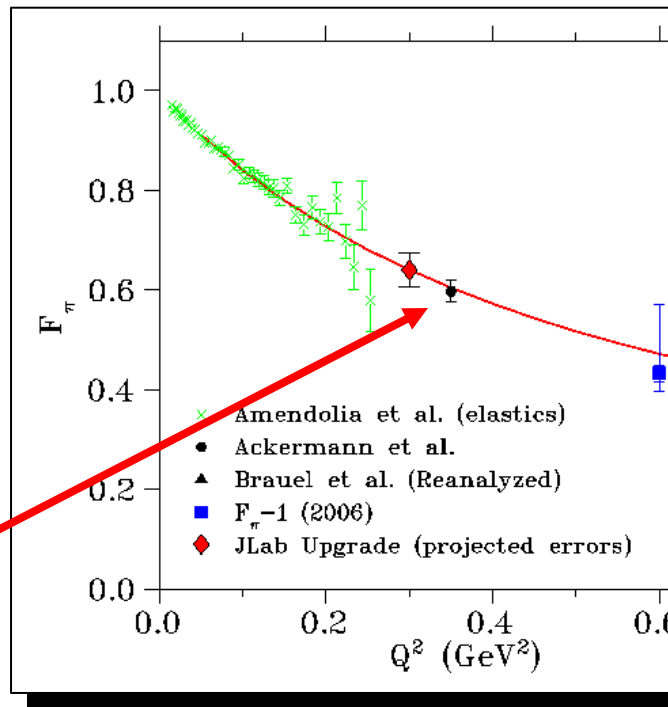


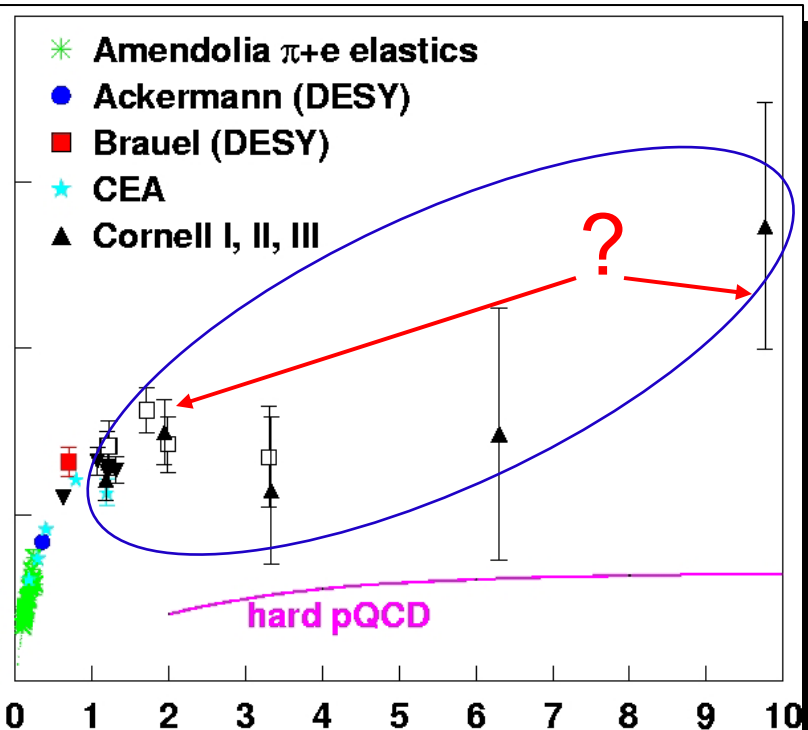
more reliable technique is to use a model including the t

Can this method yield the physical form-factor?

Test the method by comparing F_π values extracted from $p(e, e' \pi^+)n$ data with those obtained from π^+e elastic scattering at the same kinematics

ASY electroproduction data at $Q^2 = 0.35 \text{ GeV}^2$ consistent with extrapolation of elastic data [Ackerman *et al.*, *NP B277* (1986) 168]



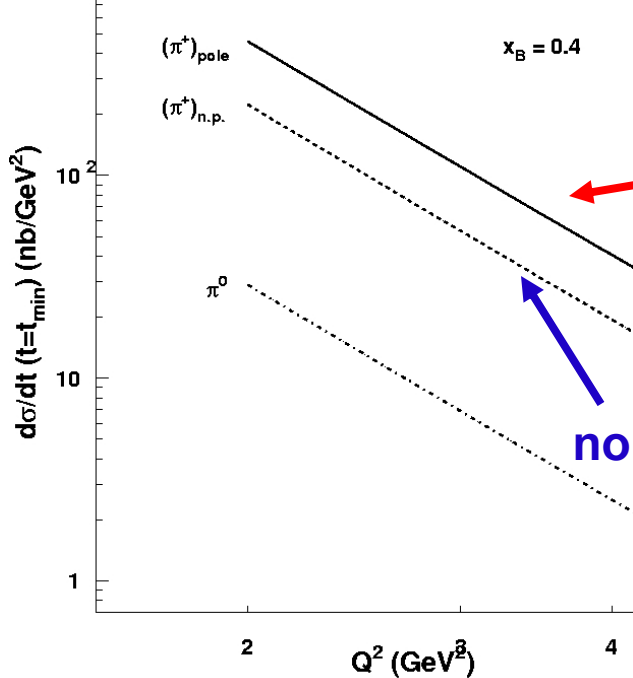


- Large Q^2 data from C
 - Use extrapolation of low Q^2 to isolate σ_{π}
 - Extract F_{π} from unscaled cross sections
- Largest Q^2 points also at large $-t$
 - Carlson&Milana prediction: $M_{\text{pQCD}}/M_{\text{pole}}$ grows significantly for $-t_m$

h of F_π measurements

Measurement of σ_L for π^0 could help
strain pQCD backgrounds

GPD framework, π^+ and π^0 cross
sections involve different combinations
of GPDs – *but π^0 has no pole
contribution*



$$(\tilde{H}^u - \tilde{H}^d)(e_+ + e_-)$$

$$A \sim (e \tilde{H}^u - e \tilde{H}^d)$$

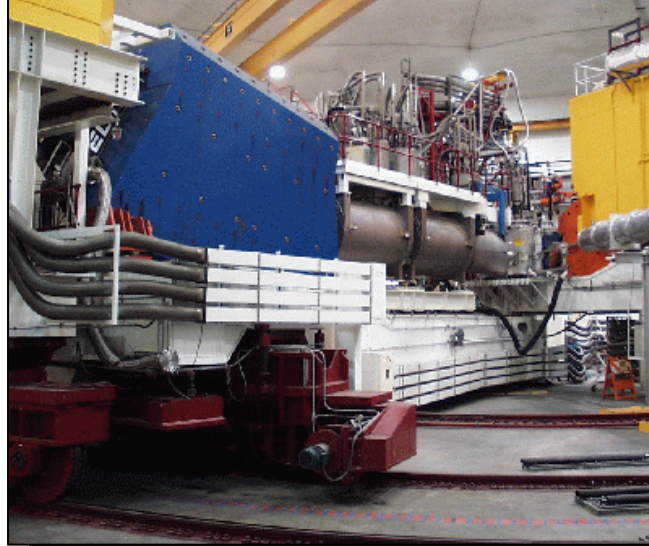
to the highest possible
of Q^2 with 6 GeV beam
Lab

F_{π^2} data at higher W ,
smaller $-t$

Repeat $Q^2=1.60 \text{ GeV}^2$ closer
to $t=m_\pi^2$ to study model
uncertainties

L/T/TT/LT separation in
production

Measurement of separated



Exp	Q^2 (GeV^2)	W (GeV)	$ t $ (GeV^2)	
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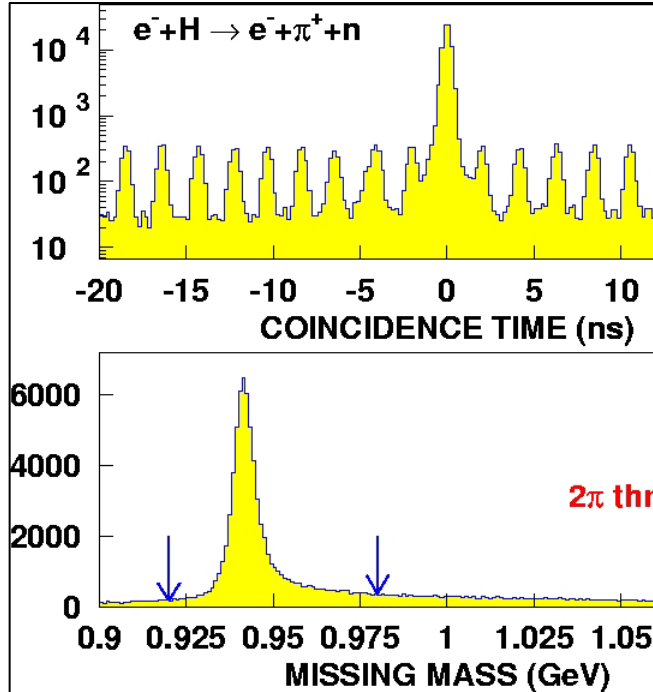
between charged pions in HMS
and electrons in SOS

- Coincidence time resolution
~200-230 ps
- Cut: ± 1 ns

protons in HMS rejected using
coincidence time and aerogel
Cherenkov

- Electrons in SOS identified by
gas Cherenkov and Calorimeter

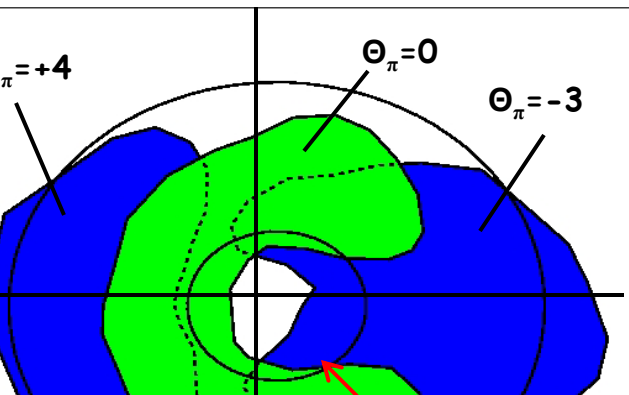
exclusive neutron final state
selected with missing mass cut



acceptance not uniform

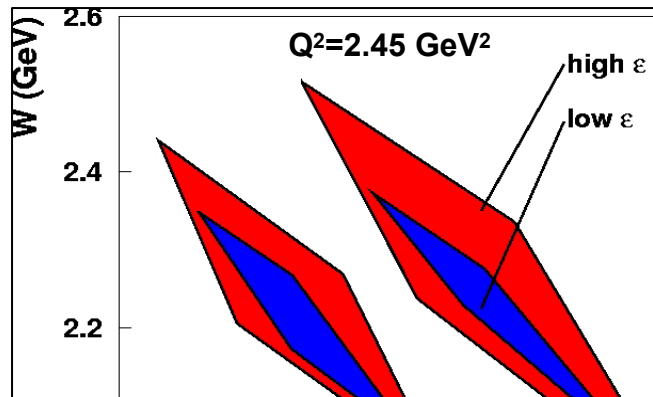
measure σ_{TT} and σ_{LT} by
taking data at three angles:
 $\Theta_\pi = 0, +4, -3$ degrees

Radial coordinate: $-t$, azimuthal coordinate: φ



at low and high ε is different

- For L/T separation use ε to define common W/Q^2 phase space



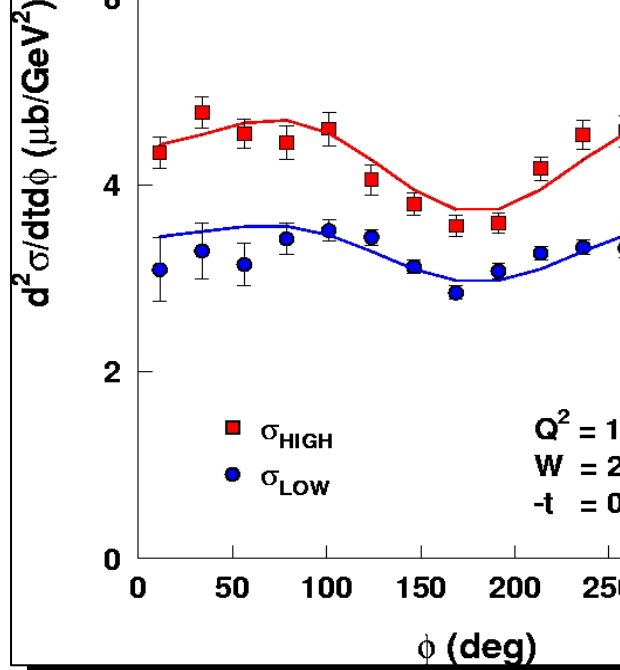
associated using the Rosenbluth separation technique

Measure the cross section at two beam energies and fixed W , Q^2 , $-t$

Simultaneous fit using the measured azimuthal angle (ϕ_π) allows for extracting L , T , LT , and TT

Careful evaluation of the systematic uncertainties is important due to the amplification in the σ_L extraction

Spectrometer acceptance, kinematics, and efficiencies



which describes pion

photoproduction in terms of

exchange of π and ρ like

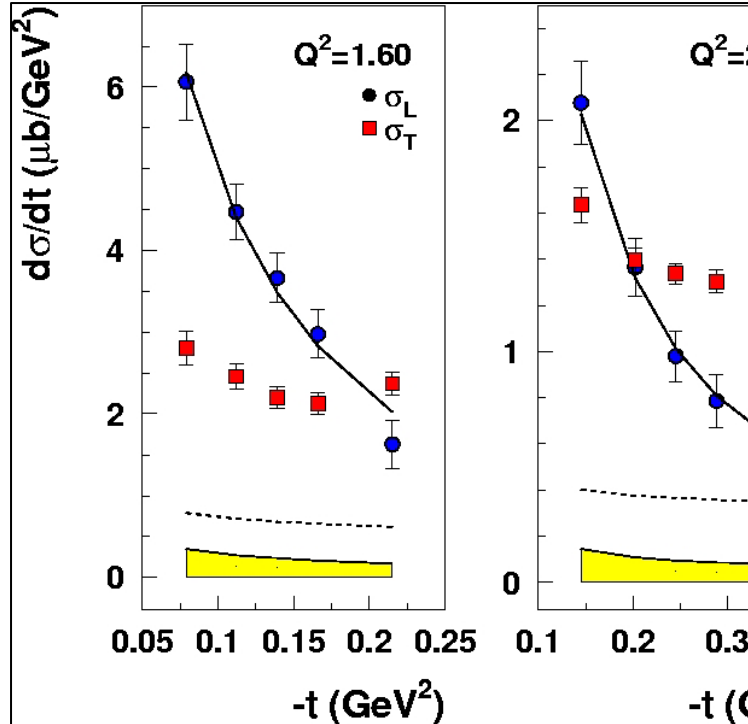
particles [Vanderhaeghen, Guidal,
et al, *PRC* **57** (1998), 1454]

Model parameters fixed from

pion photoproduction

Free parameters: F_π and F_ρ

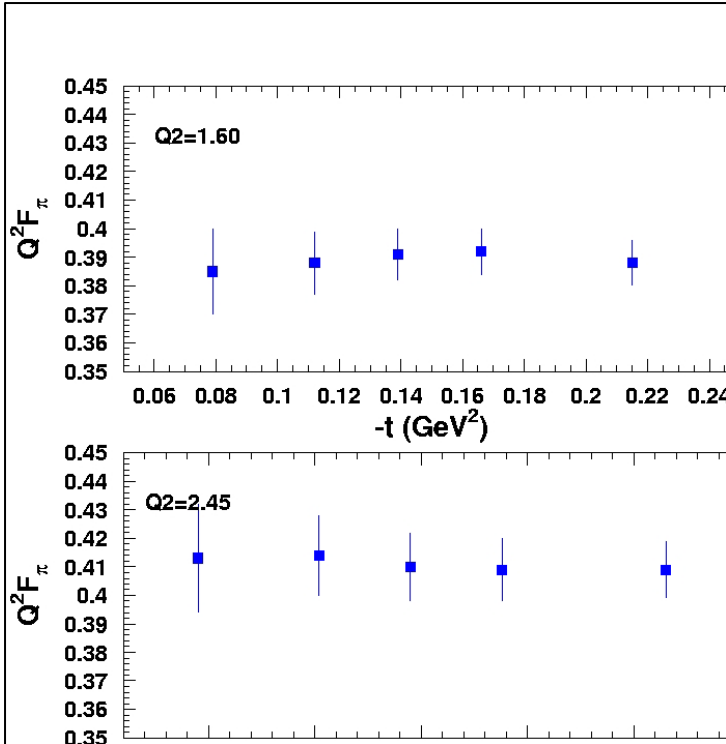
$$F_\pi = \frac{1}{1 + Q^2 / \Lambda_\pi^2}$$



Extract F_π for each t-bin
separately

F_π values are insensitive
($<2\%$) to the t-bin used

This result gives confidence in
applicability of the VGL
model in the kinematic
range of Fpi2 data



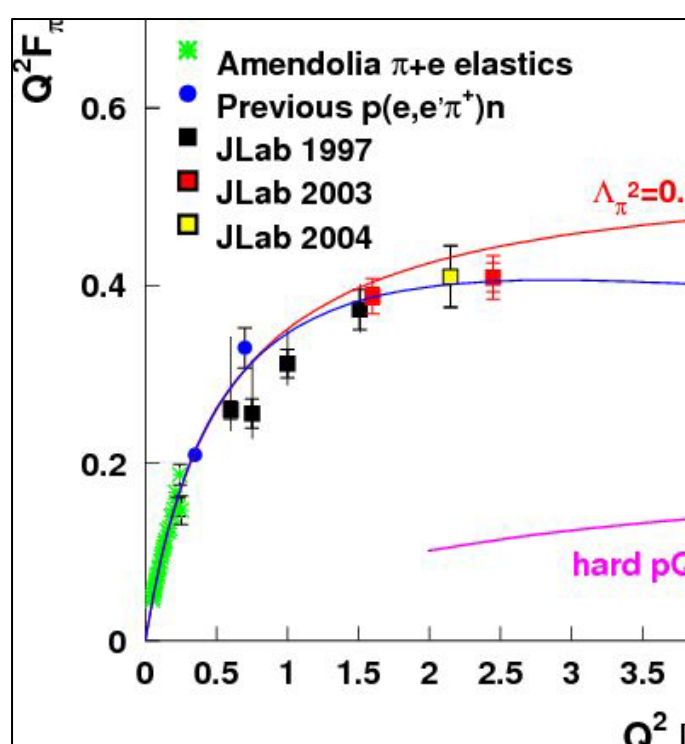
0.7 fm charge radius at $Q^2=2.45$
 Q^2 by $\sim 1\sigma$

The monopole reflects the soft (VMD)
physics at low Q^2

The deviation suggests that the π^+
“harder” at this Q^2

is still far from the pQCD
prediction

Including transverse momentum
effects has no significant impact



Nesterenko and A.V. Radyushkin, Phys. Rev. D
115 (1982)410]

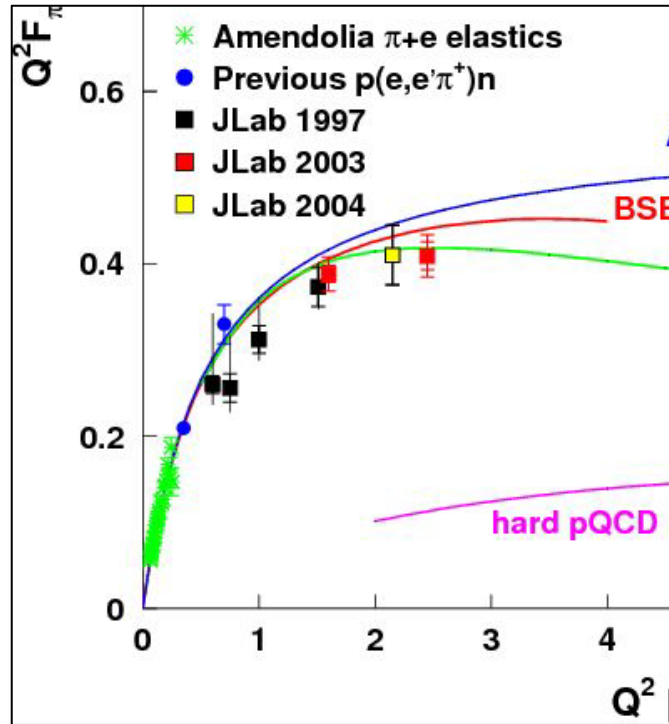
Use properties of Green functions –
spectral function contains pion pole

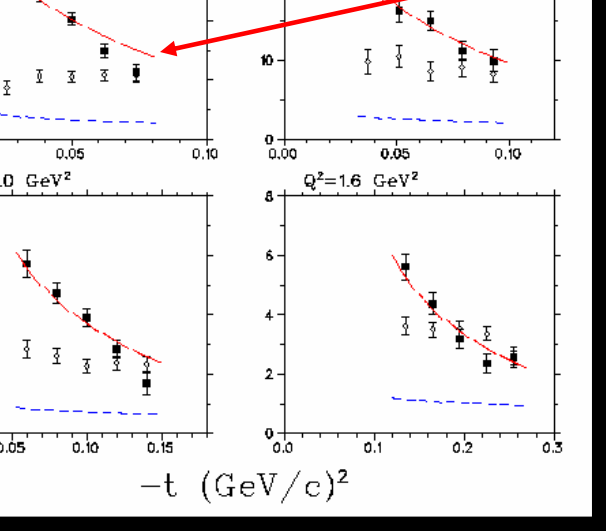
Green-Salpeter/Dyson-Schwinger

Maris and P. Tandy, Phys.Rev.C62
(2000)055204]

Systematic expansion in terms of
dressed particle Schwinger equations

de Sitter/Conformal Field Theory



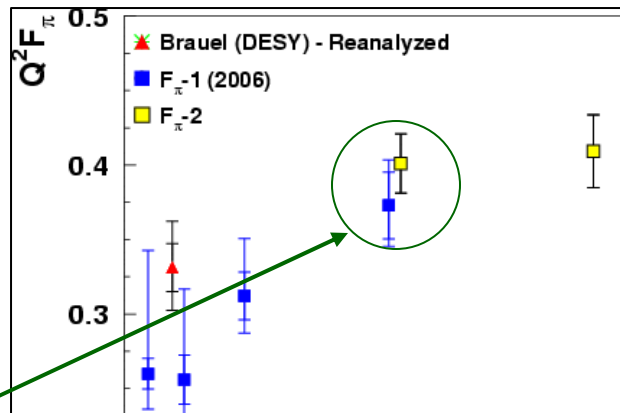


Check the model dependence of the pole extrapolation

Good agreement between $F_{\pi 1}$

at the lowest Q^2

- May be due to resonance contributions not included in
- Linear fit to Λ_π^2 to t_{\min} gives the estimate of F_π at each Q^2



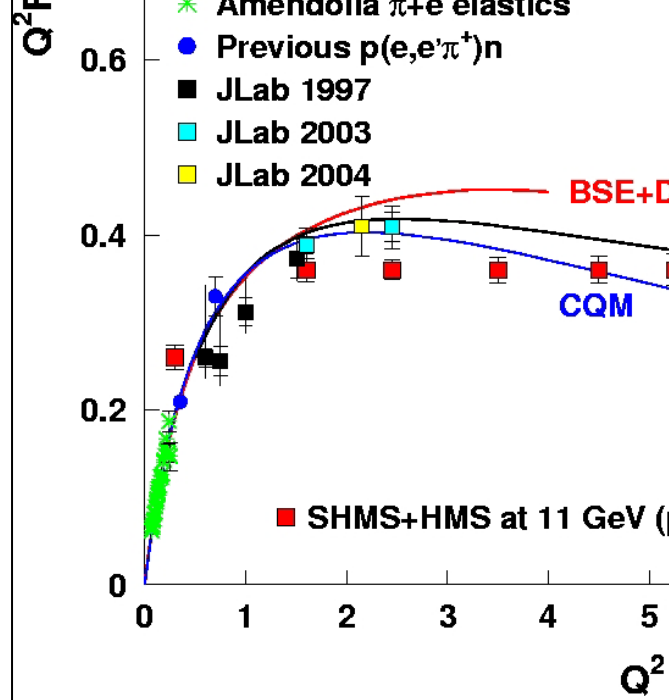
expected in next 5 years
Lattice, GPDs etc.

11 GeV electron beam and the
MS in Hall C with $\theta=5.5^\circ$ allows

Precision data up to $Q^2=6 \text{ GeV}^2$ to
study the transition to hard QCD

Test of the electroproduction
method at $Q^2=0.3 \text{ GeV}^2$ with the
upper limit of elastic scattering
data

Most stringent test of the model



dom to quarks and gluons

measurements from JLab yield high quality data – in part due to

Continuous electron beam provided by JLab accelerator

Magnetic spectrometers and detectors with well-understood properties

highest Q^2 JLab results indicate that $Q^2 F_\pi$ is still increasing, but $\sim 10\%$
monopole parameterization of the charge radius

Still far from the QCD prediction

Studies of F_π at higher electron beam energies will allow to reach the kinematic region where hard contributions are expected to dominate

Planned measurement of F_π at JLab after the upgrade to $Q^2=6 \text{ GeV}^2$

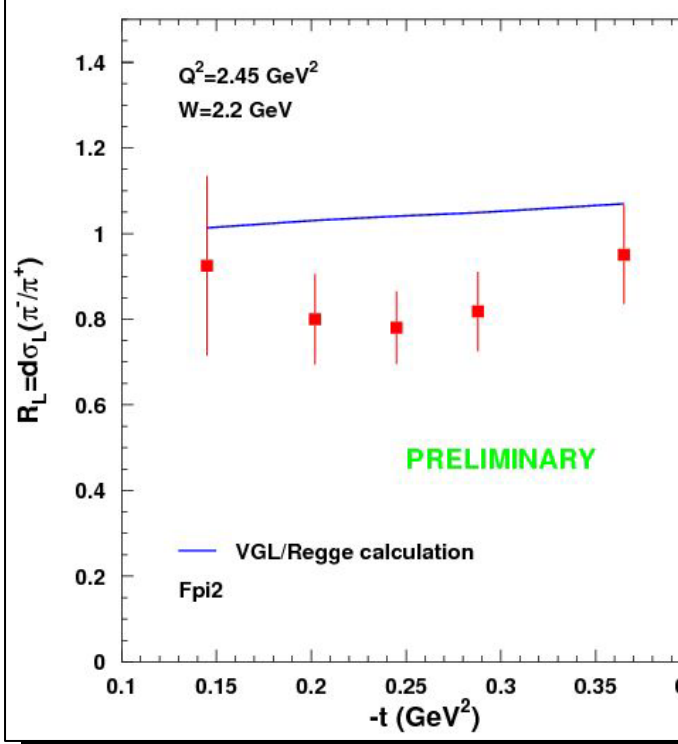
dominance of t-channel (pole dominance)

t-channel diagram is purely isovector

$$R = \frac{\sigma_L^{\pi^-}}{\sigma_L^{\pi^+}} = \frac{|A_V - A_S|^2}{|A_V + A_S|^2}$$

dominance tested using π^+ from $D(e, e'p)$

G-parity: If pure pole then necessary $R=1$

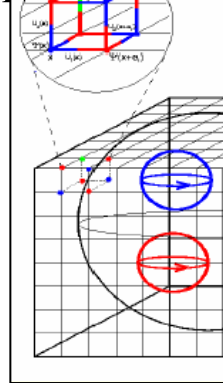


	0.1%	2.0%	0.4%
s			
orption	-	2.0%	0.1%
y	0.03%	1.0%	-
pendence	0.2%	-	1.1(1.3)%
s	0.2%	-	1.0%
king	0.1%	1.0%	0.4%
	-	0.5%	0.3%
ckness	-	0.8%	0.2%
Efficiency	-	0.5%	0.3%

Uncertainties in spectrometer quantities parameterized using constrained $^1\text{H}(e, e'p)$ reaction

- Beam energy and n to $<0.1\%$
- Spectrometer angle $\sim 0.5\text{mrad}$
- Spectrometer acceptance verified by comparing elastic scattering data to global parameterization
 - Agreement better than

must be put in by hand



LQCD requires a number of approximations

Lattice discretization errors – improved LQCD action helps

Chiral extrapolation of LQCD is used to obtain the pion mass

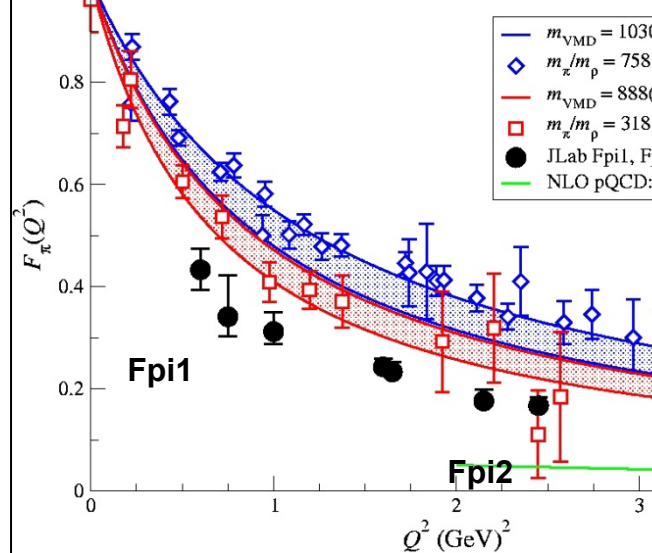
Quenching errors – need to include disconnected quark loops

Advances in computational techniques have improved over the

quenched (dynamical)
main-wall action calculation

Lattice Hadron Physics
Collaboration (Jefferson
Lab, Regina, Yale)

*F. Bonnet et al., hep-
lat/0411028*



lattice calculations are consistent with experimental data within 1% statistical and systematic errors, dominated by chiral extrapolation

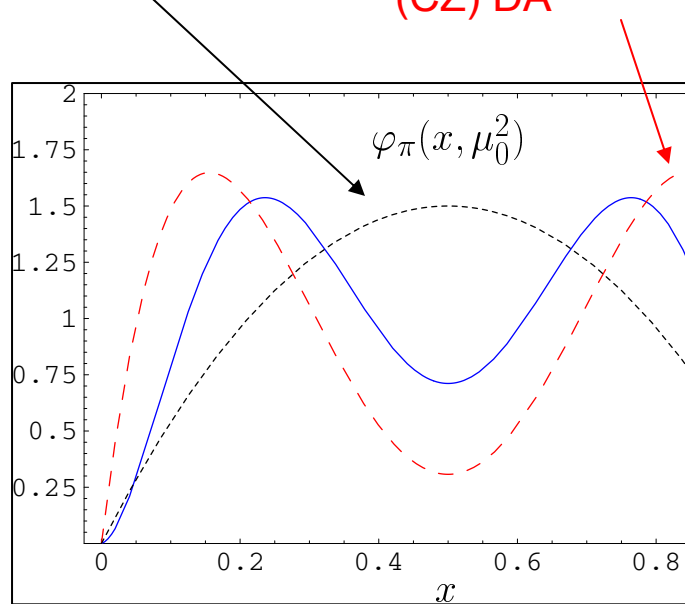
Primary goal is to test proof-of-principle of different techniques

perturbation theory at the parton
level

π DA is consistent to 1σ level
with CLEO $\pi\gamma$ transition data

results taken as evidence that
asymptotic π DA appropriate as
as $Q^2=1 \text{ GeV}^2$

F_{π^+} soft contributions from
non-perturbative hadron model need



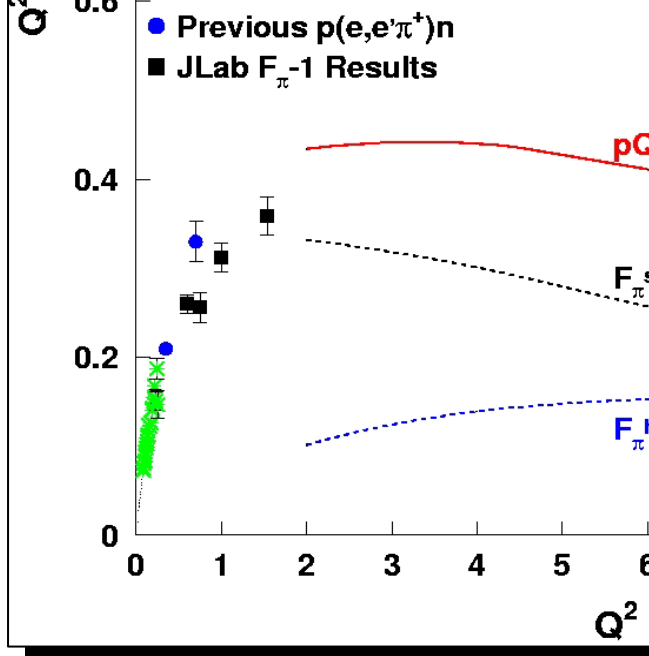
ILO

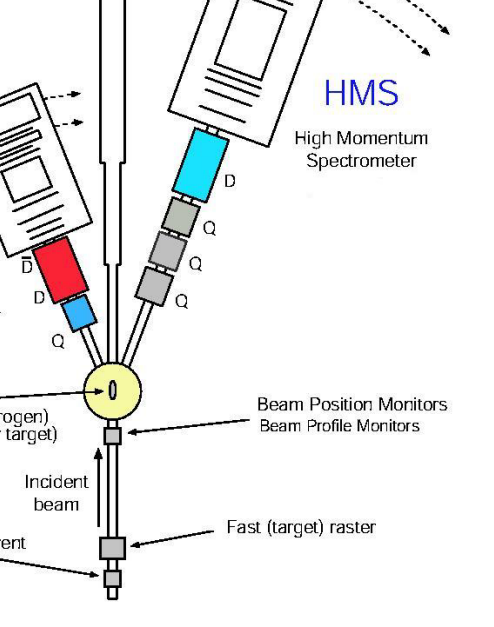
Model φ_π using QCD Sum Rules
prescription

and component significantly
over-predicts the data

To describe the data must
include soft contribution –
here, via local duality

$$F_\pi = F_\pi^{\text{soft}} + F_\pi^{\text{hard}}$$





- SOS detects e^-
- HMS detects π^+

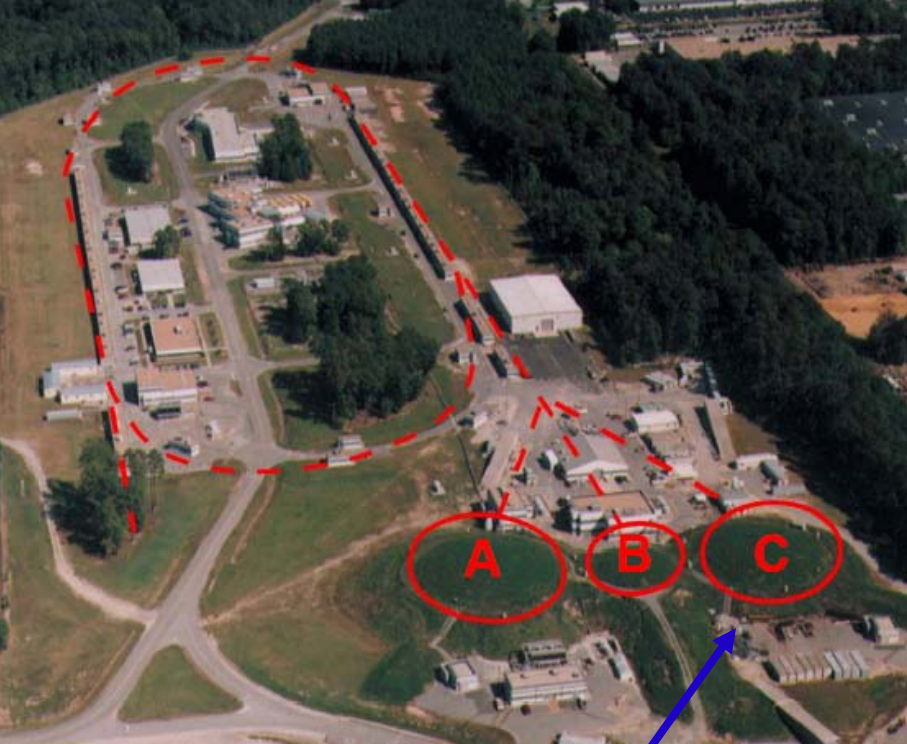
- **Targets**

- Liquid 4-cm H/D cells
- Al (dummy) target for background measurement
- ^{12}C solid targets for optics calibration

HMS Aerogel

- Improvement of $p/\pi^+/K^+$ PID momenta, first use in 2003
- Built by Yerevan group
[*Nucl. Instrum. Meth.* **A548**(2005)]

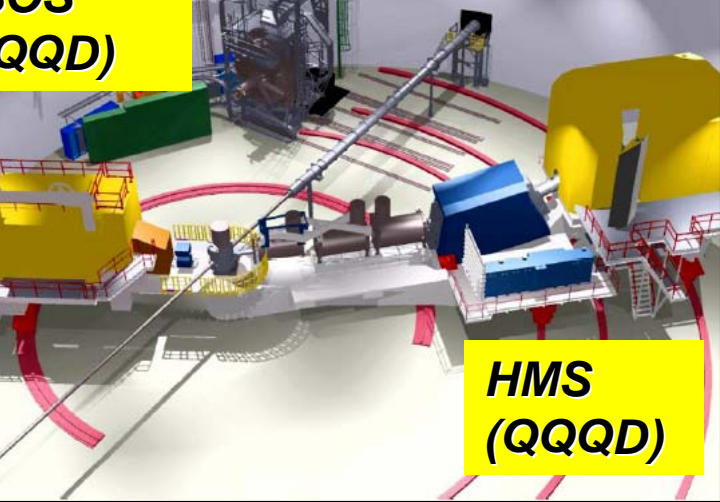




Linacs

- Three experim
Halls operatin
concurrently
- $E < \sim 5.7 \text{ GeV}$
 - Hadron-parton
transition regi
- C.W. beam with c
of up to $100 \mu\text{A}$

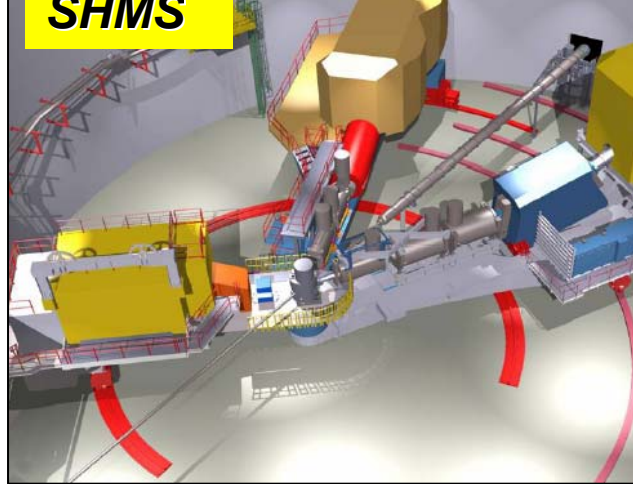
OS
(QQD)



HMS
(QQQD)

Hall C High Momentum Spectrometer and Short Orbit Spectrometer at present

SHMS



- Add a Super-High Mom Spectrometer for studies
 - Form Factors and sim